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Key Points:

- Rain affects wind wave generation and dissipation processes
- Input by wind decreases under rainy conditions
- White-capping tends to disappear under heavy rain

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Waving in the rain

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Abstract We consider the effect of rain on wind wave generation and dissipation. Rain falling on a wavy surface may have a marked tendency to dampen the shorter waves in the tail of the spectrum, the related range increasing with the rain rate. Historical and sailors' reports suggest that this leads to calmer wave conditions, certainly so for the action of breakers. We have explored this situation using a fully coupled meteorological-wave model system, adding an artificial rain rate-dependent damping of the tail. Contrarily to direct marine experience, the experimental results show higher wind speeds and wave heights. A solid indication of the truth is achieved with the direct comparison between operational model (where rain effect is ignored) and measured data. These strongly support the sailors' claims of less severe wave conditions under heavy rain. This leads to a keen analysis of the overall process, in particular on the role of the tail of the spectrum in modulating the wind input and the white-capping, and how this is presently modeled in operational activity. We suggest that some revision is due and that the relationship between white-capping and generation by wind is deeper and more implicative than presently generally assumed.

1. Wind Waves and Rain

It is a common experience among seafarers, both of the past and today, that "rain calms the sea." Figure 1 shows such a situation. The irregular surface clearly indicates that we are not dealing with swell. At the same time, for whoever had the chance to witness a stormy sea, the lack of short wave features and breakers is macroscopically evident.

The related processes have attracted scholar attention since long time ago. The first report we managed to trace back is by *Reynolds* [1875] who experimented with artificial drops falling on calm water. He reported that, if sufficiently large and energetic, each drop has a tendency to create a vortex ring and, more in general, to increase turbulence in the upper layer. He concluded saying that this had the potential of attenuating water waves. *Reynolds* [1900] came back to the subject with more details, but basically the same idea.

With few exceptions, as Manton [1973], the subject laid basically dormant, at least according to our information, for a long while. Wave modeling, entering the digital era in the 1970s, was too busy with more fundamental and quantitatively relevant processes to pay attention to rain. The matter came into focus again in the late 1980s, early 1990s, in connection with the use of remote sensing instruments, scatterometer, and Synthetic Aperture Radar (SAR) in particular. Relying for signal detection on the interaction of the emitted radar signal with the centimetric waves at the sea surface, the efficiency of the instruments was obviously depending on rain. This led to a number of studies and reported results. Tsimplis and Thorpe [1989], Tsimplis [1992], Bliven et al. [1993], Beya et al. [2010], and Peirson et al. [2013] studied the effect of artificial rain on mechanically generated waves in a wave flume and its effect on the scatterometer derived data. Poon et al. [1992], as also Braun et al. [2002], went a step further using wind generated waves in a flume with rain falling on a limited section of it. With some differences among the various reported results, the emerging general picture is the following. Rain, if intense enough as usually the case in laboratory experiments, leads to a small scale turbulence in the first few centimeters below the water surface. It also increases the surface roughness at the centimetric scale (order of frequency 10 Hz). Witnessing a downpour on a lake or a small pond will provide immediate evidence of the little messy surface. The consequent surface motion is very low, incoherent and, with the exception of an oblique rain component, isotropic. In practical terms, it does not contribute directly to wind wave generation.

© 2015. American Geophysical Union. All Rights Reserved. Longer waves, from a few centimeters upward, are attenuated. Corresponding evidence for the shorter waves, i.e., the high tail of the spectrum, is given in the various laboratory experiments quoted above. A



Figure 1. Wind sea in rainy conditions (courtesy of Ginni Callahan). Environmental conditions (onboard estimate): wind speed 15 m s⁻¹, significant wave height >1 m, mainly wind sea, very heavy rain.

quantification for the longer waves, not achievable in laboratory conditions, has been provided by *Le Méhauté and Khangaonkar* [1990, henceforth referred to as LMK] who made a keen analysis of the effect of falling rain drops on an underlying wave field, taking into consideration also the possible wind effect, i.e., of rain falling at a marked angle with respect to the vertical. For a 50 mm h⁻¹ precipitation rate (soon to be commented about), they derived a 38%, 5%, 0.5% hourly wave height decay for 1, 10, 100 m long waves, respectively.

The practical implications for scatterometer and SAR instruments have been well defined, among others, by *Weissman et al.* [2012] and

ESA [2013]. The Ku band signal (~14 GHz, 2.1 cm) is strongly affected, as it was the case for QuikSCAT. C band (~5.3 GHz, 5.6 cm) seems to fare better, and it has been the preferred choice for ASCAT. *Chen et al.* [1998] used this difference, together with radiometer data, to estimate the rain distribution on the oceans. However, according to ESA, the problem is not so well defined because the transition zone between increased and decreased wave heights, certainly in the 5–10 cm range, depends on the rain rate, the drop size distribution, the wind speed, and the time history of the rain event.

From the point of view of wave modeling, our present main interest, the seemingly accepted fact is that, when rain is present, for waves from a few centimeters upward there is a marked attenuation, rain rate dependent, and rapidly decreasing with the wave length. The case of oblique rain adding energy and momentum to waves will be discussed in section 6. For our later discussion, we will refer to LMK, as all the laboratory experiments deal with short waves and very large rain rates. For a proper perception of the relevance of the process, compare these with the typical 10 mm h^{-1} of the extratropical countries (there are local exceptions). The 50 mm h⁻¹ rates quoted in LMK and the 40 mm h⁻¹ by *Peirson et al.* [2013] (the minimum rate they used in their laboratory experiments) are already closer to local peak values. Nevertheless, the relevant seemingly accepted fact (one of us, L.C., has direct experience in this sense) is that a rainy sea has a smoother appearance than in dry windy conditions. This will be our starting point for the considerations developed in section 2. Using a state-of-the-art fully coupled meteorological-wave model system and forcing a rain rate-dependent dampening of the tail, we setup an experiment (section 3) to see how a present coupled model reacts to a high frequency smoothing of the sea surface. The results are reported in section 4. A more objective view of the situation is achieved in section 5 by a long-term comparison between operational (with no consideration of rain) and measured data. This supports the historical claims of less rough wave conditions in rainy areas, showing, however, that something is still missing in our present model coupling approach. This prompts (section 6) a keen analysis of the processes involved whose conclusions are summarized in section 7.

2. Rain Attenuates Waves in the Tail of the Spectrum

We start from the assumption in the title of this section, as derived from the above cited literature and experience, and follow the implication for wave modeling under the umbrella of the present knowledge amply applied in wind wave modeling.

Our focus is on wind wave generation. The generally accepted process, at least in operational wave modeling, is the one proposed by *Miles* [1957], and later perfected by *Janssen* [1989, 1991]. Granted the decomposition of a wavy surface into a number of spectral sinusoidal components suggested by *Pierson and Marks* [1952], Miles' mechanism envisages for each component a smooth similarly wavy air flow that, because of phase shift, ends up inputting energy to the wave. The further step by Janssen was to point out that the energy, and momentum, transferred into waves come, hence should be subtracted, from the blowing air. This must imply a slowdown of the wind field and, as immediate consequence, also lower wave heights. The direct results [*Janssen*, 1989, 1991, 2008] confirmed this approach.

A relevant detail of this process is that [*Janssen*, 2004, p. 109] "The main contribution to the wave stress is determined by the medium to high-frequency gravity waves with dimensionless speed c/u* in the range of 1–10, as these are the waves with the highest growth rate." Therefore, anything affecting the tail of the spectrum is expected to affect the interaction between atmosphere and ocean, i.e., between wind and waves.

It is clearly of interest to clarify as far as possible the physics of the involved processes when rain falls on a generative sea, and to check what our present advanced models show in these conditions. More in general, we consider a situation in which, for any external reason, the high frequency tail of the wave spectrum is cancelled. This may be because of rain, as we have described in the previous section, or because of oil on the sea surface, as done during the second world war for "men at sea" recovery in stormy conditions, or because of the mixture of water and ice in close to freezing conditions (grease ice). In this situation, the momentum input by wind to waves will be strongly reduced. The physical consequences are not obvious. It is natural to take for granted that there will be less input from wind to the sea. However, in turn, the reduced friction of the wind on the sea, together with the reduced input to waves, is likely to affect also white-capping. Being the growth and decay of a wind sea a delicate balance between these two, positive and negative, contributions, it is not straightforward to quantify in advance the final result. Following the approach by *Janssen* [1991], the matter is relevant also for the meteorological implications because a reduced input to waves will imply higher wind speeds. To analyze the situation, we make use of an advanced wave model and forecast system whose setup is the subject of the next section.

3. Modeling Setup

For our tests, we have used the coupled modeling system operational at the European Centre for Medium-Range Weather Forecasts (ECMWF, Reading, UK). The system implies a full two-way coupling between the meteorological and WAM wave models (see, respectively, *Simmons and Gibson* [2000], and *Komen et al.* [1994] and *Janssen* [2008]).

We have used the T1279 version of the system, i.e., 16 and 28 km spatial resolution, respectively, for the meteorological and wave global models. The wave model was run with 36 frequencies ($f_1 = 0.0345$ Hz) with 1.1 geometric progression, and 36 uniformly spaced directions starting at 5° clockwise with respect to North. Focused on a period to be soon specified, we have first done a reference run with the standard setup. The run was then repeated introducing a zero-ing of the wave spectrum, beyond a frequency f_c depending on the rain rate, in the calculation of the high frequency contribution to the surface stress. The rule we adopted was f_c *rain = 54, with rain (rate) given as mm h⁻¹. Whichever the rain rate, the minimum zero-ed frequency was 0.5 Hz. As previously specified, the incoherent centimeter scale surface turbulence due to rain is ignored, also because it becomes appreciable only in heavy rain conditions, when the rain attenuated spectral tail range is larger. Overall this was clearly a rather crude and arbitrary approach. For instance, it is natural to think of a progressive smoothing of the zero-ing with frequency. However, lacking any more precise indication, especially for limited rain rates, our purpose was only to explore the overall physical principles and verify in which direction the presence of the rain, or oil or grease ice, is shifting the system.

Obviously we need windy and stormy areas. This excluded the equatorial zone for lack of sustained winds. We also excluded hurricanes and typhoons as isolated and extreme events, not suitable for a first approach. We focused our attention on the North Atlantic Ocean, especially in the 35–70° latitude range (see Figure 5). Here we have frequent storms and plenty of measured data, both from buoys and satellites.

Searching for a suitable period, we have explored the wind and rain maps from January 2006 to December 2010. Our choice for a full month period was for December 2009. In this month, the ECMWF system was still running with T799 resolution (about 25 km). The archived results are regularly available at 6 h interval for analysis, 3 h for forecast. However, rain events can be shorter and spatially localized and measured data are



Figure 2. EXPerimental run with reduced surface roughness under rain versus the regular MODel results. Surface wind speeds over the North Atlantic Ocean (see Figure 5 for the considered area). Results in the (left) nonrainy areas and (right) rainy areas. Colors represent, in geometric progression, the number of cases in each pixel (see the side scale). Also the overall statistics is reported.

available in the intermediate hours. Therefore, we were interested in higher time and space resolution. Hence, in this phase, we ignored the archived data and we repeated the simulation for the full December 2009 with the already specified T1279 resolution, saving the results at 1 h interval. As said above, this was first done with the standard setup, and then repeated with the zero-ed spectral tail according to rain. Standard meteorological and wave integrated parameters and full 2-D spectra were saved at each grid point. Each run was done as a sequence of 24 h forecasts at 12 h interval. For each forecast, the 13–24 h section was retained. This provided a full month simulation suitable for the subsequent analysis.

Measured data were from moored buoy and satellite measurements. A large portion of the buoy data comes from the archive of in situ data routinely obtained from the global telecommunication system with the rest supplemented as part of the data exchanged under the JCOMM project of model performance intercomparison [*Bidlot et al.*, 2007]. Both wind and wave data were used. For the satellites, we excluded the scatterometer data because of their doubtful use in rainy areas. C band data, e.g., ASCAT, are less affected by rain and regularly used for operational purposes. However, as we will see, we deal with limited differences that would be comparable with the, albeit limited, error of the scatterometer in rainy areas. For similar, although less doubtful, reasons we excluded also the use of altimeter wind data. Altimeter wave height data seem a much more solid information. We used these data from both ENVISAT and Jason-2 satellites. The data were extracted from the RADS database [*Naeije et al.*, 2008]; see http://rads.tudelft.nl/rads/literature.shtml for details. The model results were linearly interpolated in space and time to the buoy and altimeter data.

4. Results of the Experiments

We focus our attention on the 10 m wind speed U_{10} and the significant wave height H_s as basic indicators of the performance of the coupled model system.

Figure 2 shows two scatter diagrams comparing the results from the EXP (eriment, i.e., with the zero-ed spectral tail depending on the rain rate) versus MOD (el, i.e., the standard) approach. The left panel shows the results for the nonrainy areas, the right RAIN one those for the rainy areas (in space and time). In each diagram, the dash line shows the 45° perfect fit, the continuous line through the origin the best fit to the data (symmetric slope, evaluated as $(\sum y^2 / \sum x^2)^{1/2}$). The color of the different pixel indicates the respective number of data (see the side scales). The slopes are 1.02 and 1.04 in the nonrainy and rainy areas, respectively. These figures are significant at more than 99% level. In Figure 3, we show the similar comparison for H_s against altimeter data. While in the nonrainy areas the model underestimates 6%, in the rainy areas there is a 1% excess (again this difference is significant at more than 99% level). Given the no-rain-rain differences in the two figures, we conclude that the wave height results suggest higher Hs in rainy conditions. For the time being, we refrain from any comment and explanation. We stress that the significance of these results is not in the more or less good fit with the measured data, but in the difference between dry and rainy areas. Rain is not associated to a particular zone, but it is widely distributed throughout the overall area



Figure 3. As in Figure 2, but comparison with altimeter measured significant wave heights in nonrainy and rainy areas.

bordered in Figure 5, implicitly affecting also the nonrainy zones. To further check the significance of the results in Figure 3, we have repeated the analysis for each one of the seven smaller areas, marked 1–7, in Figure 5. Stressing again the relevance of the differences between nonrainy and rainy areas, all the corresponding best fit slope differences are positive, varying between 1% and 9%, these ones too significant at more than 99%.

Having seen the general statistics, it is instructive to look at a time series of modeled rain, wind, and waves at a location during a rainy stormy event. Figure 4 shows the time evolution of the three quantities. The continuous and dash lines refer to the MOD and EXP runs, respectively. We see the increased (with respect to MOD) wind speeds and significant wave heights during the period rain is present. Note that, while the wind increase mostly represents a local effect, waves derive also from the wind action during the previous hours. Although apparently limited, the half a meter peak H_s difference is significant.

Although we did not investigate the matter further, we found that a different surface wind speed implies effects also on the upper layers of the atmosphere and in particular on the speed with which a meteorological system, typically a cold front, moves. This was verified plotting (not shown) the EXP-MOD rain rate differences across a front. Two parallel systems of large values were found, respectively, positive and negative, consequent to the different position of the front in the EXP and MOD simulations. The suggestion is that taking rain-on-wave effect into account may change the propagation speed of the meteorological fronts.

To have a more comprehensive idea of the distributed effect on modeled wave heights, we have plotted in Figure 5 the differences EXP-MOD (respectively, Exp74 and Exp73 in the title of the figure) at 09 UT of 10 December 2009. The isolines are at 10 cm interval. There is a wide distribution of positive differences, with values larger than 30 cm.



Figure 4. Four day time series of model wind speeds, significant wave heights, and rain rates at a position in the North Atlantic Ocean during December 2009. Continuous lines show the regular model results, the dash ones taking the reduced surface roughness under rain into account.

10.1002/2014JC010348

AGU Journal of Geophysical Research: Oceans



NORTH ATLANTIC - WAM WAVE HEIGHT AT 2009.12.10 09 UT (Exp74 - Exp73): CONT=positive, DOT=negative, dH=0.1m

Having shown how the meteorological and wave models react to rain "calming the sea," it is now time to explore what we can derive from the measured data. This is the subject of the next section.

5. The Comparison Between the Operational Model and Measured Data

In the previous section, we have "told" to the model that the tail of the spectrum would be flattened, at a different extent, when coming across more or less rain, and the coupled meteorological-wave model system reacted increasing, when rainy, both the wind speed and the wave height. The next step is to verify if what we have found in our experiments is indeed present also in the daily data.

For the verification, we have considered both altimeter (H_s) and buoy (U_{10} , H_s) data. Scatterometer and altimeter wind speeds have been excluded for the nonreliability of their signal in rainy areas, at least within the accuracy required for our verification. Because altimeter wave heights are assimilated into the ECMWF analysis, we have instead used the up to 12 h forecasts. This has the further advantage that the model data are available at 3 h interval (instead of the six for the analysis). To distinguish between rain and no-rain conditions, we have considered, for each time and location, the local hourly average amount of rain during the last 3 h. Thinking of the integrated effect of wave generation, we have also used the last 6 h tracking back where the local wind sea was during the previous hours. The two results, for 3 and 6 h rain, are very similar. Only the 3 h results are shown here.

The results of the comparison with North Atlantic buoy data, extended to the full 2009–2013 period, are summarized in Figure 6, top plot for the (symmetric) slope, bottom plot for the scatter index SI (rms error/mean measured value). Buoy wind data have been transformed to 10 m height assuming neutral stability conditions. The discrete values on the horizontal scales separate the various ranges of rain rate considered. The corresponding slope and SI results are plotted at the center of each range. The 0. point corresponds to the "no rain" cases. The far right RAIN point is for all the cases the rain rate is greater than 2.5 mm h⁻¹. The horizontal lines summarize all the results for rain rate >0.1 mm h⁻¹.

Figure 5. North Atlantic area considered for the present analysis. The borders are 35° and 70° North, 70° West, and 15° East. Areas 1–7 used for local statistics. Isolines (positive continuous, negative dashed) show the significant wave height differences between the experimental and the regular runs at 09 UT 10 December 2009. Isolines at 10 cm interval. Areas with more than 30 cm difference are present.



Figure 6. Intercomparison between ECMWF operational model results and buoy recorded data. Both wind speeds and significant wave heights are considered. The overall area is shown in Figure 5. The period is 2009–2013. Top panel symmetric slope, bottom panel scatter index SI. The discrete values on the horizontal scales separate the various ranges of rain rate considered. The 0 point corresponding slope and SI results are plotted at the center of each range. The 0 point corresponds to the "no rain" cases. The upper RAIN point is for all the cases the rain rate is greater than 2.5 mm h⁻¹. The horizontal lines summarize all the results for rain rate >0.1 mm h⁻¹.

With the exception of the slope for the heaviest rains (soon to be commented about), it is clear that the ECMWF operational model shows larger than measured U₁₀ and H_s values when in rainy areas. The reliability of the results decreases for high rain rates because of the limited number of cases. This is clearly shown by the vertical position of the horizontal lines summarizing all the rain cases and close to the 0.1-0.5 mm h^{-1} value. A well definite result comes from the scatter index where for both wind and waves the values increase with increasing rain. This suggests something is going on and that conditions are different under the rain.

The results are more definite for the altimeter wave heights (see Figure 7) where, consistently with Figures 2 and 3, we focus on the rainy 2009. Independently of the general slight underestimate by the model, the relevant point is that in rainy conditions the operational model provides higher wave heights with respect to the nonrainy cases. The difference is 4%, significant at more than 99%. This result holds for both December only (more and more intense rains) and for the full year. Indeed a corresponding analysis for different rain rates confirms (but with much less data in the high rate range) that the difference increases with more intense rain.

The fact that the operational model results indicate higher wave heights in





rainy areas with respect to the measured data is strongly implicative. Given that the operational model ignores the implications of rain on the spectrum, we derive that, for the same wind conditions, when it is raining the actual wave heights are lower than in similar nonrainy cases. This result is the opposite of what formerly derived from our experiments (sections 3 and 4). This demands a thorough verification and a detailed analysis of the processes at work when rain is falling on a generative area and of how they are represented in the model system.

6. The Search for an Explanation

To summarize the previous results, the situation is the following. The operational model ignores the effect of rain. A direct comparison between its results and the measured data has shown that indeed wave heights are appreciably lower in rainy areas (and therefore the model overestimates them). However, when "told" that rain is present by flattening the spectral tail, the model reacts in the opposite (larger wave heights), hence wrong, direction. In this section, we explore in sequence the various aspects of the processes at work trying to find what is wrong or missing in the model approach. We stress again that all our reported statistics, exemplified in the intercomparisons in Figures 2, 3, and 7, are very robust. We double-checked their significance using both the boot-strap and the jack-knife approaches [see e.g., *Edgington*, 1995]. All the results turned out significant at better than 99%.

6.1. The Direct Effect of Rain Attenuating Wave Height

We start with the simple, well acknowledged evidence that "rain calms the sea." While, as already specified, with this expression sea-men really mean the disappearance of the breaking crests, it is correct to try to quantify how much the rain can effectively dampen the sea. Practically, to obtain measurable results within a laboratory distance, all the related experiments had to work with very high rain rates, well above what experienced in the sea (with the exception of extreme cases). Also very short wave lengths had to be considered. Given the strong sensitivity of the attenuation to the wavelength, these results, although interesting from the physical point of view, are not very useful to evaluate the attenuation in the field main wave regime. For this, we have reported the results of the theoretical approach of *Le Méhauté and Khangaonkar* [1990, LMK] who again worked with substantial rain rates. With 50 mm h⁻¹, they found a H_s attenuation of 38, 5 and 0.5% h⁻¹ for 1, 10, 100 m wavelength, respectively. Assuming these figures hold also when composed in a spectrum, considering, e.g., an 8 s peak period JONSWAP one, a quick estimate suggests an overall Hs decrease of 1.2% h⁻¹. Extrapolation (that we expect nonlinear) of these figures to the more common 10–30 mm h⁻¹ of a cold front and to wave period of 10 s or more typical of the North Atlantic winter suggests a figure less than 0.5% h⁻¹, i.e., that rain is not the direct responsible (factor) for a substantial decrease of wave height leading to the disappearance of breakers.

6.2. Rain Affects the Presence of White-Caps

Nevertheless, we cannot neglect the perception that after a sustained rain we perceive (measurements are scarce in these conditions) that the wave heights are somehow lower. However, the key point we need to stress is that the disappearance, or decreasing number, of whitecaps under a strong rain is practically an instantaneous process (matter of seconds). The steep waves in Figure 1 are suggestive in this respect. The picture was taken in the Tahiti area during a squall. Being a localized event, model data, referred to a wider area, do not represent the specific conditions. The people onboard reported wind speed larger than 15 m s⁻¹ and significant wave height higher than 1 m. As also evident from the picture because of wave steepness, dominant waves were locally generated. Rain was reported as "very heavy." One of us (L.C.) has recently witnessed such an event during a wave measuring campaign on the ISMAR oceanographic tower (Northern Adriatic Sea, 16 m depth, 15 km offshore the Venice coast). Figure 8 pictures the situation, with $H_s = 1.4 \text{ m}$, at 3 min difference, soon after and before the onset of the downpour (32 mm h⁻¹ recorded on board). No marked variation of wind (about 14 m s⁻¹) was evident from the local records. Videos for the two situations are available as well. Clearly some different basic physics is at work.

Following LMK, some physical intuition and some keen experiments as by *Peirson et al.* [2013], it is clear that rain acts mainly and more effectively on the tail of the spectrum. It is then natural to assume that what we see in a downpour, i.e., the disappearance of the whitecaps, is related to the different situation in the tail. This is supported by the results of *Hwang and Wang* [2004] suggesting that a strong signature of wave



Figure 8. Sea surface and white-capping distribution during and just before a violent and sudden downpour (32 mm h^{-1}). The two pictures have been taken at less than 3 min distance. Significant wave height 1.4 m, wind speed 14 m s⁻¹. Oceanographic tower of ISMAR, 16 m depth, 15 km offshore Venice, Italy.

breaking is found in the 0.16–2.1 m wavelength scale. The related distribution in the field is not random, but, as direct evidence strongly suggests, mostly associated to the crests of the dominant waves.

6.3. How Rain Affects Wind Input to Waves

A stronger effect turns out to concern the key element of any sea storm, i.e., the wind input to waves. The basic theory was formulated by Miles [1957, plus a later sequence of papers], then refined by Janssen [1989, 1991] to consider the feedback of waves on the driving wind field. The theory stands on three basic concepts, those of roughness length z_0 (i.e., the height close to the surface where the wind speed is null), of a logarithmic vertical profile of the wind speed, and of critical height z_c as the one where wind speed equals the phase speed of the wave component we consider acting upon. Most of the drag of the wind profile, hence a large momentum flux from wind to waves, is given by the tail of the spectrum with its low but steep waves, hence the low values of z_0 . If these waves are flattened by rain z_0 increases (now related to longer and higher waves), and the logarithmic profile, so to say, relaxes, with a less steep increase of the wind speed close to the surface. In turn, this implies a substantial increase of the critical height z_c for all the frequencies of the spectrum. This has a dramatic effect on the input by wind to the considered component because the momentum transfer to waves is roughly proportional to $exp(-2kz_c)$ with k the wave number (see the discussion by Lighthill [1962]). Indeed the Miles-Janssen mechanism is effective only for low values of the critical height with respect to the wavelength. This makes the input to the bulk of the spectrum extremely sensitive to the condition of the tail. Following the above argument a heavy rain, via its effect on the tail, indirectly affects the whole generation process. Because during generation most of energy input by wind (>90%) is immediately lost as white-capping [see e.g., Holthuijsen, 2007], cancelling the tail leads also to an immediate decrease, in the extreme the disappearance, of white-capping.

So the tail of the spectrum acts on surface breaking in two ways: via the direct influence of the tail on the breaking process, and via the possible drastic decrease of input by wind. In this second aspect, it is worth mentioning that there is a feedback process at work. In 1976, Banner and Melville pointed out that much, if not most, of the momentum input by wind to waves does not take place as a smooth continuous process. Rather, it happens in bursts, mostly in connection with the breakers, or white-caps, that characterize the crests of a sea under the vigorous action of wind. *Kudryavtsev and Makin* [2001] further explored this possibility evaluating the form drag associated to the presence of breakers. *Babanin et al.* [2007], following their AUSWEX experiment, concluded that the presence of breakers implies a significant phase shift in the local wave-coherent surface pressure. This produces a wave-coherent energy flux from wind to waves with a mean value twice the corresponding energy flux to the nonbreaking waves. So the decreased input by wind because of rain is further decreased because of the reduced white-capping.

6.4. The Modifications of the Nonlinear Interactions

Another point to be discussed is the modification of the nonlinear interactions balance once the tail of the spectrum is flattened. Still sticking for simplicity to the classical JONSWAP spectrum of a generating sea, we know (see, for instance, the detailed and keen analysis by *Young and Van Vledder* [1993]) that there is a flow

of energy from the central part of the spectrum toward higher frequencies where it is dissipated by whitecapping. If we zero the tail, the nonlinear interactions will tend to reestablish the "correct" spectral shape. In practice, there will be an increased flow of energy from the central part of the spectrum toward the tail. A first-hand estimate is obtained estimating the energy cancelled by rain and the consequences on the overall energy and the associated significant wave height. Using again the figures provided by LMK, we obtain a figure close to 1%, far from the values required to justify the overall situation. A more precise estimate has been obtained with the full evaluation of the related Boltzmann integral using ExactNL. Also this result indicates that the flow of energy toward the tail cannot justify a rapid appreciable decrease of the significant wave height. In any case, the test has also highlighted how approximate is in this case the Discrete Interaction Approximation (DIA) [*Hasselmann et al.*, 1985] used every day in operational modeling.

6.5. The Effect of Oblique Rain and Wind Torn Crests

With respect to the direct action of rain on wind waves, we need to consider (see LMK) that, if sufficiently intense and falling at an angle, rain can add energy and momentum to waves. A similar argument concerns the foaming crests under a strong wind when their tearing leads to large, rapidly accelerated water drops impinging on the back side of the previous wave. The argument is subtle because the energy and momentum of the flying rain or drops are extracted from the wind. In the case of rain *Manton* [1973] has roughly quantified the loss of wind speed at the 10^{-3} level. While the overall energy of the system (rain, drops, and wind) remains the same, we should possibly consider that their direct impinging on the previous wave can be a more efficient way of transferring energy from air to waves. The subject, at least in certain conditions, deserves attention. It is remarkable that even the single effect of rain on the wind is presently not considered in the operational meteorological models (A. Beljaars, personal communication, 2014). This can, and probably will, be a subject of future research, but it does not seem to be, at least in the large majority of cases, the explanation for the results shown in Figure 6.

6.6. The Definition of Sea Surface in Very Strong Wind Conditions

Two things need to be pointed out about the effect of rain or torn drops on waves. The nice machine we have assembled in a numerical wave model assumes a clean well defined separation surface between air and water. However, when we go to very high wind speeds, the obvious examples being hurricanes, the separation surface begins to lose its meaning, substituted by a layer of "foaming material," troughs full of foam, and so on. The physics of this interface, still a subject of valuable studies [see e.g., *Soloviev and Lukas*, 2010], is different, and it is amazing that our wave models still manage to produce valuable results also in these conditions. Remaining on more solid (or liquid) ground, in this paper, we deal with less extreme conditions exploring the direct effect of rain on wave generation.

6.7. Rain in the Present Meteorological Models

Focusing on the meteorological aspect of rain, it is relevant that, as cited above, the horizontal momentum of rain is presently not considered in meteorological modeling (A. Beljaars, personal communication, 2014). More in general, the water cycle, and more specifically the rain rate, is still open to improvement in meteorological modeling (see e.g., http://old.ecmwf.int/publications/library/do/references/show?id=90901). In particular, the present ECMWF model has a tendency to drizzle, i.e., to overpredict very low rain rates. For this reason, we have excluded this lower range from our analysis. Another important aspect is that, independently of the model accuracy, a once-an-hour or once-every-three-hour integrated rain datum is likely to smooth or average the truth. Rain comes often in bands, a very patchy process, both in space and time, with rapid and alternating variations. If the process considered is nonlinear, to apply the overall average to the process under consideration may lead to a different result. On the other hand, this is the information we have at disposal and have to work with. In a way, the situation is similar to wind gustiness in wave modeling. Abdalla and Cavaleri [2002] showed that, following the standard approach to the generation by wind, a gusty wind leads to higher wave heights than using its average value. At least on the average, the problem was partially solved having an estimate of the level of gustiness and, knowing the related physics, deriving a parameterized estimate of the implication [Janssen, 2008]. Somehow, having an estimate of the rain patchiness, the same approach could be followed for the implications for wind and waves.

6.8. The Effect of White-Capping

On a parallel criticism on wave modeling, we need to realize that white-capping is still the least understood process in wave modeling, for this reason often used as the tuning knob of the system. A somehow opposite, but solid physical approach to the process of white-capping was given by *Banner et al.* [2002] who pointed out how the single crests may reach breaking conditions as a consequence of the energy convergence while reaching the top of the enclosing envelope. However, at the model scale much simpler approaches are used [see e.g., *Bidlot*, 2012; *Ardhuin et al.*, 2010] based on the shape of the spectrum, but not very sensitive to the presence of the tail. Unluckily no detailed wave spectra exist taken under rainy conditions, certainly not in the frequency range high enough to observe the behavior of the tail in these conditions. Physically, based on theory, experiments and intuition, it is reasonable to expect, while the rain rate increases, a progressively larger section of the tail to be affected, starting from the high frequency end and gradually extending toward the lower frequencies. In turn, this will affect the white-capping more and more, again starting from the crests of the shorter waves, and progressively extending to the ones of the longer and dominant waves (as it is the case in Figure 1).

6.9. Why the Model Reacts in the Wrong Direction

In the previous section 5, and more so in our experiment in section 4, we have seen that (a) the operational model ignores the effect of rain on the tail of the spectrum, in so doing leading to larger than truth wave heights in rainy conditions, (b) even when (our experiment) we "tell" to the system that the tail is dampened, rather than reducing, this leads to even larger wave heights. This requires an explanation. In the ECMWF system, the surface wind speed depends on the drag at the surface, drag that includes the momentum flux to the spectral tail (a large part of the whole). A dampened tail, hence a reduced drag, leads to an increased surface wind speed. However, contrarily to what described in 6.3, the model wind vertical profile shape is not changed. This implies a stronger input to the lower, nondampened, part of the spectrum, with the consequent increase of the significant wave height. The obvious correction is in a tighter coupling between atmosphere and ocean with a modification of the wind vertical profile according to the full details of the wave spectrum. Work is planned in this direction.

7. A Final Picture of the Basic Process at Work

In the previous section, we have analyzed in sequence different aspects of the interaction between a blowing wind and the associated generative wave conditions. Clearly, the physics of the interface is multifaceted, depending on the scale of approximation we have in mind. In this paper, we have focused on the macroscopic evidence that under a windy rain the sea grows less, if at all, and that, the more spectacular effect, the white-caps tend to disappear within a fraction of a minute, if not in a matter of seconds. Although various physical aspects can be at work at different (smaller) scales, we offer the following description of the basic process at work.

Rain, if sufficiently intense, and as done with oil especially in the past, dampens the high frequency part of the wave spectrum. With increasing rain rate, the dampening begins in the capillary range extending progressively, but with progressively longer time scale, to lower frequencies. The smoother surface leads to a lower friction of wind on the surface, in so doing reducing the slowdown due to wave coupling and their growth rate. However, we find also an increase of the roughness length and of the critical height in the *Miles-Janssen* generation process. This strongly reduces the input by wind on the whole spectral range. Because most of the wind input to a growing sea is immediately lost as white-capping, this implies also a much reduced breaking rate. With time passing, and rain continuing, the height and steepness of the waves tend to decrease, but it is important to realize that the decreased generation and number of breakers are immediate effects at the onset of rain (if sufficiently intense). The two facts, reduced generation and break-ing, loop on each other because breaking enhances wind input via the possible detachment of the surface layer at the crest.

In the present meteorological-wave coupled systems (as at ECMWF) [*Janssen*, 2008], the shape of the wind vertical profile does not adapt to the reduced drag of the tail consequent to rain, oil, or grease ice on the surface. This implies that the *Miles-Janssen* generation process continuous unabated, leading to excess wave heights in the operational model, and, more so, in our experiment.

A second practical problem for the proper consideration of the above process in wave modeling is the approximation still present in rain forecast, both because of its patchiness and the uncertainties that still characterize the water cycle in meteorological modeling. For the former, a statistical approach similar to what done for wind gustiness can be a possible solution.

Because at the onset of a heavy rain the white-capping disappears vary rapidly (matter of seconds or little more), the wave spectrum does not change drastically across this short transient. This suggests that the present white-capping quantification in wave modeling, related to the distribution of energy in the spectrum, is not fully correct. Historically, the evolution of wave field (in deep water) has been conceived as the result of three different processes: wind input, nonlinear interactions, and white-capping. We suggest that wind input and white-capping should be considered as a single process. Indeed, in engineering terms, the present approach may appear difficult and illogical. Wave growth is evaluated as a minor difference, almost 2 orders of magnitude smaller, between two large quantities, wind-input and white-capping, independently evaluated, the latter one still considered not properly known (hence its use as a tuning knob). This is prone to errors. Given the physical connection between the two processes, we suggest that a new approach, based on a single view of these two strongly connected, but presently separate, processes, is the way to follow in the future. Remarkable indications, as the ones by Banner and Melville [1976] and Kudryavtsev and Makin [2001], had already shown the reciprocal influence of white-capping and generation. However, although in an undefined way for which we beg the reader pardon, we feel that a more unified concept and definition, physical and numerical, is required. White-capping and generation, both not existing without the other one. Both crucial for all the exchanges (mass, energy, heat, momentum, etc.) between atmosphere and ocean. So crucial not only for the single storm, but also for the Earth climate. An updated, more solid, and complete approach is badly required.

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